

5.1 Extra Practice

In Exercises 1–3, find the indicated real n th root(s) of a .

1. $n = 3, a = 343$

2. $n = 6, a = -64$

3. $n = 5, a = -243$

In Exercises 4–9, evaluate the expression without using technology.

4. $36^{3/2}$

5. $16^{3/4}$

6. $(-32)^{2/5}$

7. $(-125)^{5/3}$

8. $256^{-5/4}$

9. $27^{-4/3}$

In Exercises 10–15, evaluate the expression using technology. Round your answer to two decimal places, if necessary.

10. $28^{-1/5}$

11. $150^{2/5}$

12. $40,351^{6/7}$

13. $750^{-2/5}$

14. $(\sqrt[5]{223})^3$

15. $(\sqrt[7]{-34})^5$

In Exercises 16–21, find the real solution(s) of the equation. Round your answer to two decimal places, if necessary.

16. $6x^4 = 60$

17. $x^5 = -233$

18. $x^4 + 19 = 100$

19. $x^3 + 17 = 57$

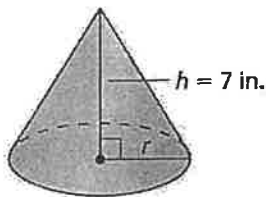
20. $\frac{1}{5}x^4 = 125$

21. $\frac{1}{7}x^3 = -49$

In Exercises 22 and 23, find the radius of the figure with the given volume.

22. $V = 425 \text{ in.}^3$

23. $V = 1458 \text{ m}^3$



24. Kepler's third law states that the relationship between the mean distance d (in astronomical units) of a planet from the Sun and the time t (in years) it takes the planet to orbit the Sun can be given by $d^3 = t^2$.

- It takes Venus 0.616 year to orbit the Sun. Find the mean distance of Venus from the Sun (in astronomical units).
- The mean distance of Jupiter from the Sun is 5.24 astronomical units. How many years does it take Jupiter to orbit the Sun?

5.2 Reteach (continued)

The Power of a Product and Power of a Quotient properties can be expressed using radical notation when $m = \frac{1}{n}$ for some integer n greater than 1.

Key Idea

Properties of Radicals

Let a and b be real numbers such that the indicated roots are real numbers, and let n be an integer greater than 1.

Property Name	Definition	Example
Product Property	$\sqrt[n]{a \cdot b} = \sqrt[n]{a} \cdot \sqrt[n]{b}$	$\sqrt[3]{4} \cdot \sqrt[3]{2} = \sqrt[3]{8} = 2$
Quotient Property	$\sqrt[n]{\frac{a}{b}} = \frac{\sqrt[n]{a}}{\sqrt[n]{b}}, b \neq 0$	$\frac{\sqrt[4]{162}}{\sqrt[4]{2}} = \sqrt[4]{\frac{162}{2}} = \sqrt[4]{81} = 3$

EXAMPLE Using Properties of Radicals

Use the properties of radicals to simplify each expression.

a. $\sqrt{5} \cdot \sqrt{45} = \sqrt{5 \cdot 45} = \sqrt{225} = 15$ Product Property of Radicals

b. $\frac{\sqrt[3]{108}}{\sqrt[3]{4}} = \sqrt[3]{\frac{108}{4}} = \sqrt[3]{27} = 3$ Quotient Property of Radicals

In Exercises 1–6, use the properties of rational exponents to simplify the expression.

1. $(7^2)^{1/4}$

2. $(14^3)^{1/2}$

3. $\frac{5^{1/5}}{5}$

4. $\frac{10}{10^{1/4}}$

5. $\left(\frac{6^5}{9^5}\right)^{-1/5}$

6. $(7^{-3/4} \cdot 7^{1/4})^{-1}$

7. $(2^3 \cdot 6^6)^{1/6}$

8. $(5^3 \cdot 3^3)^{-2/3}$

9. $\frac{(9^{2/3})^3}{(3^{1/3})^3}$

In Exercises 10–18, use the properties of radicals to simplify the expression.

10. $\sqrt{3} \cdot \sqrt{75}$

11. $\sqrt[3]{81} \cdot \sqrt[3]{9}$

12. $\sqrt[4]{12} \cdot \sqrt[4]{8}$

13. $\sqrt[4]{9} \cdot \sqrt[4]{9}$

14. $\frac{\sqrt[3]{128}}{\sqrt[5]{4}}$

15. $\frac{\sqrt{5}}{\sqrt{80}}$

16. $\frac{\sqrt[3]{375}}{\sqrt[3]{3}}$

17. $\frac{\sqrt[4]{405}}{\sqrt[4]{5}}$

18. $\frac{\sqrt{5}}{\sqrt{125}}$