1.2

Enrichment and Extension

Transformations of Linear and Absolute Value Functions

In Exercises 1–6, write a function g whose graph represents the indicated transformations of the graph of f(x) = 2x - 1. Then find the x-intercept of the graph of g. Use technology to check your answers.

- 1. translation 3 units right followed by a translation 1 unit down
- 2. translation 1 unit left followed by a reflection in the x-axis
- 3. vertical stretch by a factor of 3 followed by a translation 3 units down
- **4.** horizontal shrink by a factor of $\frac{1}{3}$ followed by a translation 5 units up
- 5. translation 3 units right followed by a vertical stretch by a factor of 2
- 6. translation 1 unit up followed by a reflection in the x-axis and a translation 3 units left

In Exercises 7–12, write a function g whose graph represents the indicated transformations of the graph of f(x) = |x + 2| - 1. Then find the x-intercept(s) of the graph of g. Use technology to check your answers.

- 7. translation 3 units right followed by a translation 1 unit down
- 8. translation 1 unit left followed by a translation 2 units up
- **9.** translation 1 unit up followed by a reflection in the x-axis and a translation 3 units left
- **10.** translation 1 unit right followed by a vertical stretch by a factor of 2 and a translation 4 units down
- 11. horizontal shrink by a factor of $\frac{1}{4}$ followed by a translation 10 units right and 1 unit up, and a reflection in the x-axis
- 12. translation 5 units right followed by a translation 3 units down, a vertical shrink by a factor of $\frac{1}{2}$, and a reflection in the x-axis



Why Did The Computer Sneeze?

Write the letter of each answer in the box containing the exercise number.

Write a function g whose graph represents the indicated transformation of the graph of f.

1.
$$f(x) = x + 4$$
; translation 3 units left

2.
$$f(x) = x - 7$$
; translation 5 units right

3.
$$f(x) = |2x - 5| + 3$$
; translation 2 units up

4.
$$f(x) = -4x - 8$$
; reflection in the x-axis.

5.
$$f(x) = |2x + 1| - 6$$
; reflection in the y-axis

6.
$$f(x) = -x + 5$$
; horizontal shrink by a factor of $\frac{1}{2}$

7.
$$f(x) = |2x - 4|$$
; vertical stretch by a factor of 4

Write a function g whose graph represents the indicated transformations of the graph of f.

- 8. f(x) = x; vertical stretch by a factor of 3 followed by a translation 2 units down
- **9.** f(x) = x; translation 1 unit up followed by a vertical shrink by a factor of $\frac{1}{4}$
- **10.** f(x) = |x|; reflection in the x-axis followed by a translation 2 units right
- 11. f(x) = |x|; vertical shrink by a factor of $\frac{1}{2}$ followed by a translation 5 units up and 1 unit left

Answers

R.
$$g(x) = \frac{1}{4}x + \frac{1}{4}$$

U.
$$g(x) = -|x-2|$$

T.
$$g(x) = x - 12$$

H.
$$g(x) = |2x - 5| + 5$$

A.
$$g(x) = -2x + 5$$

A.
$$g(x) = 4x + 8$$

S.
$$g(x) = \frac{1}{2}|x+1| + 5$$

D.
$$g(x) = |-2x + 1| - 6$$

$$\mathbf{I.} \quad g(x) = 3x - 2$$

$$\mathbf{I.} \quad g(x) = x + 7$$

V.
$$g(x) = 4|2x - 4|$$

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