## Core Algebra 2



Midterm Review

## Chapter 1 Review

There will be 38 questions on the midterm exam. Graph the function and identify the function, then describe the transformations of functions.

1. $f(x)=x+3$

2. $f(x)=2(x+1)^{2}-3$

3. $h(x)=\frac{1}{2} x^{2}$

4. $h(x)=\frac{1}{2}(x+2)^{2}+1$

5. $f(x)=-|x|-3$

6. $f(x)=-3(x-1)^{2}-2$

7. Write a function $g$ that is a translation 4 units right and 6 units down, followed by a reflection about the $x$-axis of the graph of $f(x)=-\frac{1}{2}(x+1)^{2}$.
8. Write a function $g$ that is a translation 3 units left and 4 units up, followed by a reflection about the $x$-axis of the graph of $f(x)=(x+3)^{2}$.
9. Write a function $g$ that is a translation 2 units right and 6 units up, followed by a v . stretch of 2 of the graph of $f(x)=-(x-3)^{2}-2$.
10. Write a function $g$ that is a translation 3 units left and 2 units down, followed by av. shrink of $\frac{1}{2}$ of the graph of $f(x)=2(x+1)^{2}+4$.
11. Write a function $g$ that is a translation 2 units left and 3 units down, $v$. stretch of 3 , followed by a reflection about the $x$-axis of the graph of $f(x)=-2(x+1)^{2}-1$.
12. Write a function $g$ that is a translation 4 units right and 5 units up, v . shrink of $\frac{1}{2}$, followed by a reflection about the $x$ axis of the graph of $f(x)=4(x+1)^{2}-3$.

## Write a function $g$ whose graph represents the indicated transformations of the graph of $f$ for \#13-16.

13. $f(x)=x$; vertical stretch by a factor of 3 .
14. $f(x)=-3 x+4$; translation 3 units down followed by a reflection about the $x$-axis.
15. $f(x)=2|x|-9$; translation 2 units left and 6 units up followed by a vertical shrink by a factor of $\frac{1}{3}$.
16. $f(x)=\frac{1}{2}(x+2)^{2}-5$; vertical stretch by a factor of 2 followed by a translation of 4 units right.
17. Use the graph to write an equation of the line and interpret the slope.


Find the slope of the following points.
18. $(3,-5)(5,-9)$
19. $(-6,10)(-4,7)$
20. $(1,8)(-3,8)$
21. $(-2,7)(8,11)$
22. $(-4,6)(4,-3)$
23. $(-2,3)(-8,6)$

Write the linear equation in slope-intercept form for each given set of information for \#24-32.
24. $m=\frac{2}{3}(3,6)$
25. $(-2,5),(-1,1)$
26.

| $x$ | $y$ |
| :---: | :---: |
| -4 | 2 |
| -1 | 1 |
| 2 | 0 |
| 5 | -1 |

27. $m=2,(-1,4)$
28. $(5,9),(3,13)$
29. $(-3,7),(-1,7)$
30. The table shows the numbers of ice cream cones sold for different outside temperatures (in degrees Fahrenheit). Do the data show a linear relationship? If so, write an equation of a line of fit and use it to estimate how many ice cream cones are sold when the temperature is $60^{\circ} \mathrm{F}$.

| Temperature, $x$ | 53 | 62 | 70 | 82 | 90 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Number of cones, $y$ | 90 | 105 | 117 | 131 | 147 |

Solve the system of equations by graphing.
31. $3 x+y=3$
$4 x+2 y=2$
32. $2 x+2 y=6$
$3 x+y=1$
33. $-x+2 y=-1$
$2 x-3 y=3$

Solve the system of equations by substitution.
34. $2 x-3 y=-10$
$3 x+y=7$
35. $3 x-2 y=5$
$x+3 y=9$
36. $2 x-y=-8$
$4 x+3 y=4$

Solve the system of equations by elimination.
37. $2 x+y=6$
$-3 x-2 y=-8$
38. $3 x-2 y=4$
$4 x+3 y=11$
39. $x+3 y=6$
$3 x+2 y=4$

## Chapter 2 Review

Describe the transformation of $f(x)=x^{2}$ represented by $g$. Then graph each function.
40. $g(x)=-\frac{1}{2} x^{2}$

42. $g(x)=2(x-1)^{2}$

44. $g(x)=-\frac{1}{4} x^{2}+3$

41. $g(x)=-3(x+2)^{2}-1$

43. $g(x)=4(x+3)^{2}+1$

45. $g(x)=-(x-4)^{2}-5$


## Write a rule for $g(x)$.

46. The graph of $g$ is a vertical stretch by a factor of 3 , followed by a translation 5 units right of the graph $f(x)=x^{2}$.
47. The graph of $g$ is a translation 2 units left and 3 units up, followed by a refection about the $x$-axis of the graph $f(x)=x^{2}-2$.
48. The graph of $g$ is a translation 3 units right, 2 down, and a vertical stretch by a factor of 3 of the graph $f(x)=x^{2}$.
49. The graph of $g$ is a translation 5 units left and 4 units up, followed by a refection about the $x$-axis of the graph $f(x)=(x+1)^{2}$
50. The graph of $g$ is a translation 4 units left and 3 units down, followed by a refection about the $x$-axis of the graph $f(x)=(x-2)^{2}+4$
51. The graph of $g$ is a translation 3 units right and 2 units down, vertical shrink by a factor of $\frac{1}{2}$, followed by a refection about the $x$-axis of the graph $f(x)=(x-2)^{2}+4$
52. The graph of $g$ is a translation 4 units left and 5 units down, vertical stretch by a factor of 3 , followed by a refection about the $x$-axis of the graph $f(x)=(x-1)^{2}+2$
53. The graph represents the path of a football kicked by a player, where $x$ is the horizontal distance (in yards) and $y$ is the height (in yards). The player kicks the ball a second time so that it travels the same horizontal distance, but reaches a maximum height that is 6 yards greater than the maximum height of the first kick. Write a function that models the path of the second kick.


Graph the function. Label the vertex and axis of symmetry. Find the minimum value or maximum value of the function.
54. $f(x)=3(x-1)^{2}-4$

56. $f(x)=-2(x+3)^{2}+6$

55. $h(x)=(x-3)(x+7)$

57. $h(x)=(x+4)(x-2)$


## Write the equation of the parabola with the given characteristics.

58. Write a quadratic function in standard form with a vertex of $(3,2)$ and $y$-intercept of 20 .
59. passes through ( $-2,3$ ), and has a vertex of ( $-4,7$ ).
60. Passes through $(4,3)$ and has $x$-intercepts -1 and 5 .
61. passes through $(4,11)$, and has a vertex of $(2,3)$.
62. Passes through $(1,4)$ and has $x$-intercepts -2 and 6 .
63. passes through $(2,-5)$, and has a vertex of $(-2,-1)$.
64. Passes through $(3,4)$ and has $x$-intercepts 0 and 8 .
65. passes through $(5,1)$, and has a vertex of $(3,-1)$.
66. Passes through ( $-1,-6$ ) and has $x$-intercepts -5 and 3 .

Factor (these will not be on the Exam but need to review and practice).
67. $x^{2}-7 x+12$
68. $x^{2}-36$
69. $x^{2}+10 x-24$
70. $3 x^{2}-6 x+9$
71. $2 x^{2}+9 x-5$
72. $x^{2}-10 x+25$

